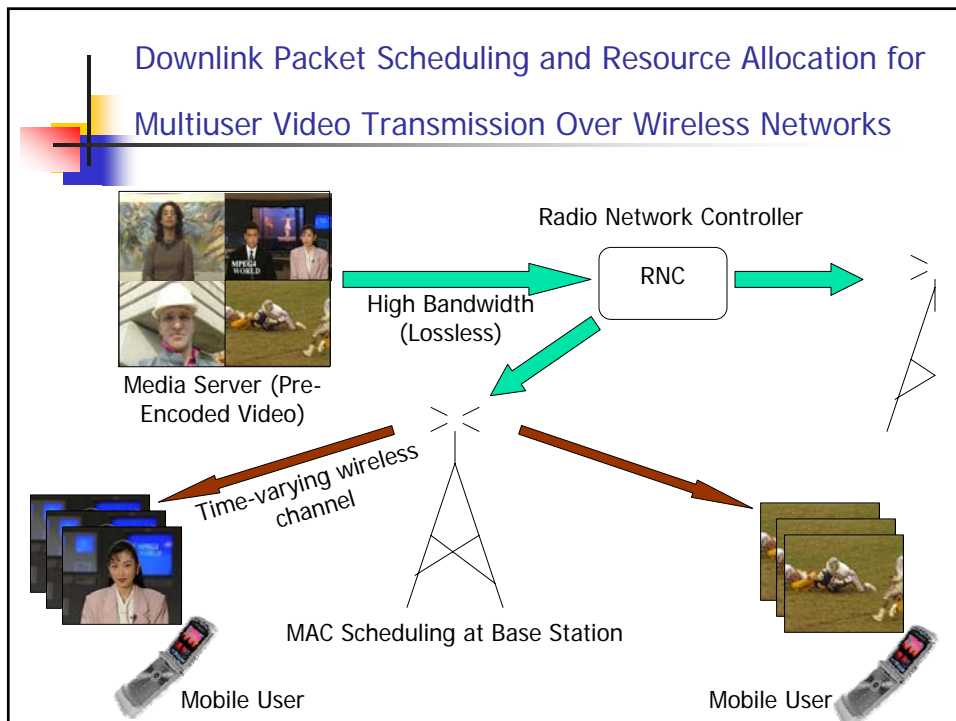


# CASE III

## Downlink Packet Scheduling and Resource Allocation for Multiuser Video Transmission Over Wireless Networks





## Scheduling and Resource Allocation

- General Problem Definition
  - Transmit multiple pre-encoded video sequences
  - To multiple users
  - Over 3G/4G wireless networks
  - Find optimal distribution of resources at base station
  - Such that each user receives a reasonable quality of service
- Limited Resources (limits achievable data rates)
  - Transmission power
  - Number of spreading codes (Bandwidth)
- Quality of Service Measures
  - End-to-end distortion of video sequence
  - Transmission delay (stringent requirement for real-time applications)



## Advancements in Wireless Networks

### High Speed Downlink Packet Access (HSDPA)

- CDMA/TDM
  - 5 MHz bandwidth, 2ms time slots
- Fast Scheduling at Base Station
  - MAC scheduling at 2ms time slot
  - Dynamically adapt to channel conditions
- Adaptive Modulation and Coding
  - QPSK and 16 QAM
  - Rate 1/3 Turbo codes, variable with *puncturing* and *repetition*
- Fast Hybrid ARQ
  - Chase Combining
  - Incremental Redundancy

### IEEE 802.16e (Mobile WiMAX)

- OFDMA/TDM for Multiple Access
  - 5 -10 MHz bandwidth,
- Fast Scheduling at Base Station
  - MAC scheduling at 5ms time slots
- Adaptive Modulation and Coding
  - QPSK, 16 QAM, 64 QAM
  - Variable rate convolutional turbo codes
- Fast Hybrid ARQ



## Downlink Packet Scheduling

- “Dumb” Method
  - Round Robin
- State of the Art
  - **Basic Idea:** Allocate resources to users with better channel quality
  - Maximum Throughput Methods
  - Proportionally Fair Methods
    - Fairness criterion based on current average throughput
  - Gradient Based Scheduling
    - Maximize rate to users that will gain the most, subject to channel conditions
- Scheduling for Streaming Video
  - Minimize queue length (delay of head-of-line packet)
  - **Current work does not consider rate-distortion trade-offs for individual video packets**

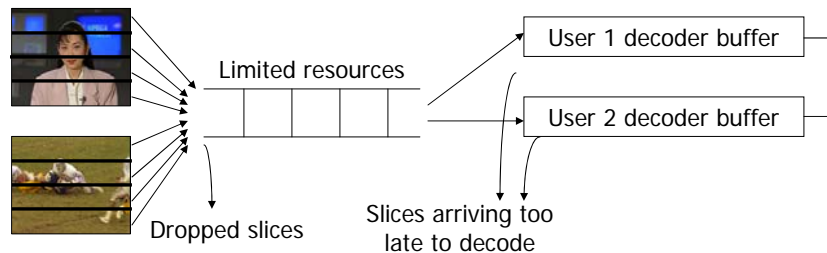


## Downlink Scheduling- Background

- Channel Independent
  - Round robin scheduling for TDM (e.g., 2G GSM networks)
- State of the Art – Channel Dependent
  - Exploit multiuser diversity
    - Maximize throughput
  - Maintain fairness across users
    - Proportionally fair
    - Gradient-based scheduling techniques
- Scheduling for Streaming Video
  - Queue-length / delay based QoS metrics
  - **Current techniques are content independent**
- **Proposed Technique**
  - **Content-aware packet scheduling** for wireless video streaming

## Video Transmission Assumptions

- Frames are split into **independently decodable slices**
- Video will be viewed in **real-time** (slices from the current frame must be received by the decoder before it finishes decoding the previous frame)
- **Achievable data rates** may not be sufficient to transmit every slice of every frame to all the users within the real-time constraints



## Key Ideas

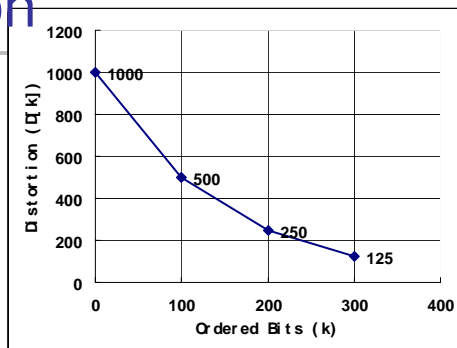
- Define **importance** of a packet based on distortion reduction achieved by transmitting the packet
- **Order** video packets by importance
- Generate **distortion-based utility function**
- Consider **error concealment** at the decoder which conceals losses due to dropped packets
  - Simple concealment : Copy MB from the same position in previous frame
  - Complex concealment (described later) adds dependencies between slices/packets

# Formulation

- Key Idea
  - Order slices by amount of distortion reduction
  - Define Slice Utility in terms of distortion reduction
- Assumptions
  - Channel states may change by an order of magnitude over one frame's duration
    - Feedback is available every 2ms in HSDPA
    - Optimization performed every time slot (2ms)
  - Simple error concealment
    - Copying MB from the same position in previous frame
    - Complex error concealment adds dependencies between slices
      - complicates slice ordering
    - Will eventually include complex error concealment

# Utility Function

- Utility Per User Based on Slice Ordering
  - $D[k] :=$  Distortion given  $k$  slices are received
  - $D[M] =$  Minimum distortion where,  $M =$  total # of slices



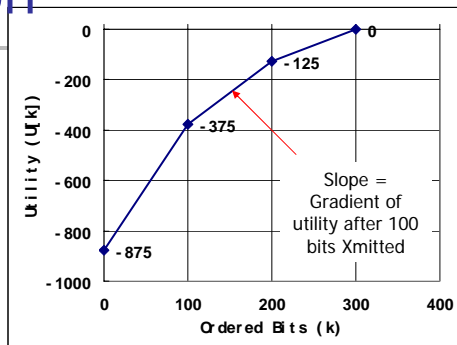
Distortion vs bits after slice ordering

# Utility Function

## Utility Per User Based on Slice Ordering

- $D[k] :=$  Distortion given  $k$  slices are received
  - $D[M] =$  Minimum distortion where,  $M =$  total # of slices
- $$U[k] = (D[M] - D[k])$$

$$u[k] = U'[k] = \frac{D[k] - D[k+1]}{B_{k+1}}$$



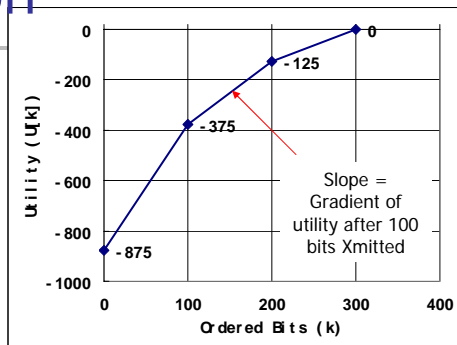
Utility vs bits after slice ordering

# Utility Function

## Utility Per User Based on Slice Ordering

- $D[k] :=$  Distortion given  $k$  slices are received
  - $D[M] =$  Minimum distortion where,  $M =$  total # of slices
- $$U[k] = (D[M] - D[k])$$

$$u[k] = U'[k] = \frac{D[k] - D[k+1]}{B_{k+1}}$$



Utility vs bits after slice ordering

- Gradient Based Scheduling – Maximizes rates per user weighted by gradient of utility function

$$\max \sum_{i=1}^K w_i u_i \cdot r_i$$

$K$  : # of users  
 $r_i$  : rate per user  
 $w_j$  : fairness weighting

## HSDPA System Constraints

- K users
- Maximum transmission power:  $\sum_{i=1}^K p_i \leq P$ 
  - $p_i :=$  power per user
- Number  $n_i$  of codes per user:  $n_i \leq N_i$
- Total number of spreading codes:  $\sum_{i=1}^K n_i \leq N$
- Achievable rates:  $r_i = n_i \Gamma(\xi_i \cdot SINR_i)$ 
  - $SINR_i := \frac{p_i}{n_i} e_i$
  - Where  $e_i :=$  channel state (SINR per unit power)
  - $\Gamma :=$  Shannon capacity assuming Gaussian noise channel
  - $\xi_i \in (0, 1] :=$  gap from capacity

## Problem Definition

- Maximize sum of user rates weighted by utility gradients:

$$V^* = \max_{\mathbf{n}, \mathbf{p}} \sum_{i=1}^K w_i u_i \cdot n_i B \log \left( 1 + \frac{p_i e_i}{n_i} \right)$$

$$\text{subject to : } \sum_{i=1}^K n_i \leq N \quad \text{additional constraint : } n_i \leq N_i$$

$$\text{and } \sum_{i=1}^K p_i \leq P$$

## Solution

Define Lagrangian

$$L(\mathbf{n}, \mathbf{p}, \lambda, \mu) = \sum_{i=1}^K w_i u_i \cdot n_i B \log \left( 1 + \frac{p_i e_i}{n_i} \right) + \lambda \left( P - \sum_{i=1}^K p_i \right) + \mu \left( N - \sum_{i=1}^K n_i \right)$$

Define Dual Function

$$L(\lambda, \mu) = \max_{(\mathbf{n}, \mathbf{p}) \in C'} L(\mathbf{n}, \mathbf{p}, \lambda, \mu)$$

Solve Dual Problem

$$L^* = \min_{(\lambda, \mu) \geq 0} L(\lambda, \mu)$$

$$L^* = \min_{\lambda \geq 0} L(\lambda) \quad \text{where, } L(\lambda) = \min_{\mu \geq 0} L(\lambda, \mu)$$

Can find  $\lambda$  using bisection search

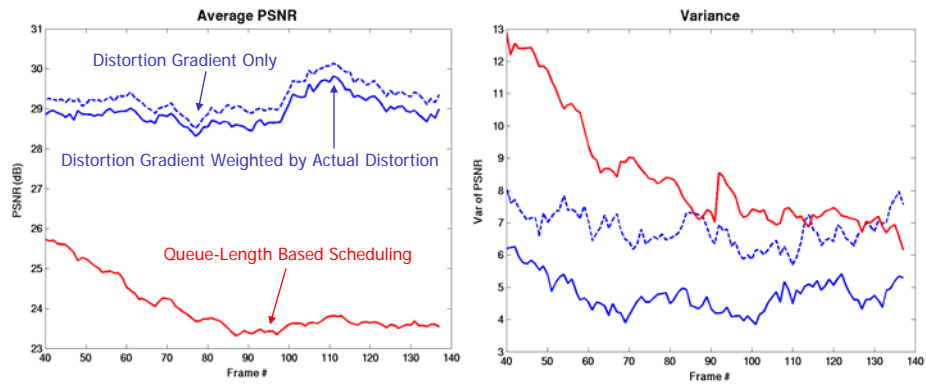
R. Agrawal, V. Subramanian, and R. Berry, "Joint Scheduling and Resource Allocation in CDMA Systems," *IEEE Trans. on Information Theory*

## Simulation I : Similar Fading Stats

- HSDPA System
  - # of Users ( $K$ ) = 12
  - Total # of spreading codes ( $N$ ) = 15
  - Max codes per user ( $N_i$ ) = 5
  - Total Power ( $P$ ) = 9.9W
  - Max SINR = 1.59 dB
  - Simulated uncorrelated Rayleigh fading channels, with same average channel conditions, for each user
- Video Source
  - H.264 encoded at 256kbps
  - QCIF (176x144) {foreman, mother and daughter, carphone, news, silent, news, 0...139, 150...289}
  - 11 MBs per slice



# Simulation I Results



# Demo 1

- 6 users
- $P = 7W$



Weighted Distortion Gradient Metric

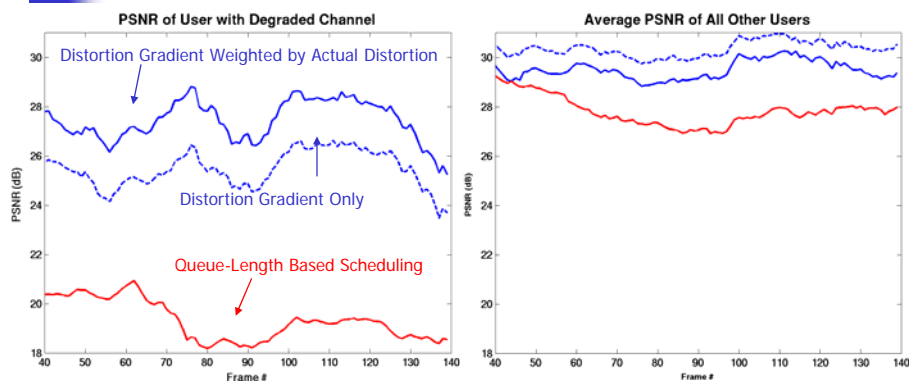


Queue-based Utility Metric

## Simulation II : One Degraded User

- HSDPA System
  - # of Users ( $K$ ) = 10
  - Total # of spreading codes ( $N$ ) = 15
  - Max codes per user ( $N_i$ ) = 5
  - Total Power ( $P$ ) = 9.9W
  - Max SINR = 1.59
  - Simulated uncorrelated Rayleigh fading channels, with one user having lower average channel quality
- Video Source
  - H.264 encoded at 256kbps
  - QCIF (176x144) {foreman, mother and daughter, carphone, news, silent, 0...139, 150...289}
  - 11 MBs per slice

## Simulation II Results



- The weighted distortion gradient tends to be fair to all users while not significantly sacrificing overall quality

## Demo 2

### Reception Quality for User with Degraded Channel

Distortion-based Utility



Queue length-based Utility



## Additional Considerations

- Complex error concealment
  - Incremental gain not additive
  - Myopic solution
  - Smoothed utility gradient
- Use of a scalable bitstream
- Random Packet Losses



## Simulations

- Channel Statistics
  - Realistic HSDPA channel traces obtained from simulators at Motorola assuming users are 0.8 km from base station traveling at 30 kmph
  - Results averaged over 5 channel realizations, 100 frames per sequence
- System Parameters
  - # of users ( $K$ ) = 6
  - Total # of spreading codes ( $M$ ) = 15
  - Max codes per user ( $N_i$ ) = 5
  - Total power ( $P$ ) = 10W
  - Max SINR ( $\hat{S}_i = 1.8\text{dB}$ )
- Video Source (6 sequences)
  - H.264 encoded with average PSNR of 35dB for each sequence
  - QCIF (176x144) {foreman, mother and daughter, carphone, news, silent}
  - 11 MBs per slice

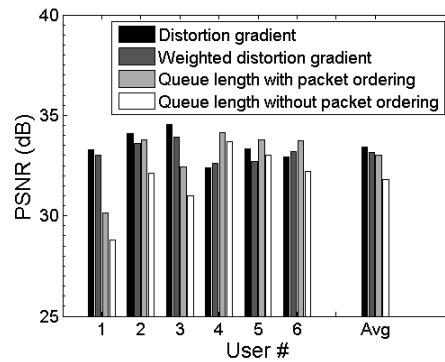


## Results: Comparison of Metrics

$$\max_{(\mathbf{n}, \mathbf{p}) \in C} \sum_{i=1}^K w_i u_i \cdot r_i(\mathbf{n}, \mathbf{p})$$

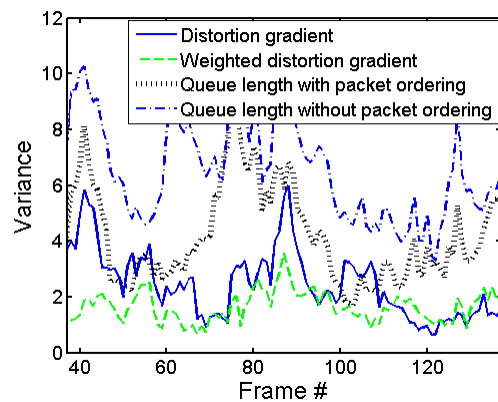
- Distortion Gradient
  - Proposed technique ( $w_i = 1$ )
- Weighted Distortion Gradient
  - Proposed technique ( $w_i =$  current distortion of sequence)
- Queue Length
  - Conventional content-independent technique
  - Replace  $w_i u_i$  with # of bits remaining in frame for user  $i$
  - Equivalent to utility function of form  $(-Q^?)$ , found in conventional buffer management techniques
- Ordered Queue
  - Proposed packet ordering technique without content-dependent resource allocation
  - Same as Q but first, order the slices in each frame by distortion gradient

## Results – Average PSNR



- 1: Foreman
- 2: Mother and daughter
- 3: Car phone
- 4: News
- 5: Silent
- 6: Hall Monitor

## Results – Variance of PSNR



- The ordered queue method performs just as well as the distortion gradient methods on average but causes higher variability in quality across users

## Demo

WDG  
33.1dB

Ordered Queue  
30.0dB

Queue  
28.6dB



32.6dB

34.0dB

33.6dB

## Formulation with Random Pkt Losses

- Order Video Packets by Importance
  - Based on **expected** reduction in distortion achieved by transmitting the packet
- Allocate Resources to Packets/Users with Larger Expected Distortion Gradients
- Consider **Error Concealment** at the Decoder
- Channel Model
  - Packet loss rates can be modeled as a function of estimated channel quality and allocated resources

# Expected Distortion Calculation

Expected distortion of frame n

$$E[D_n] = \frac{1}{N} \sum_{i=1}^N E\left\{ \left( f_n^i - \tilde{f}_n^i \right)^2 \right\}$$

Number of pixels      Actual value of  $i^{\text{th}}$  pixel (Known)      Decoded value of  $i^{\text{th}}$  pixel (Random due to channel loss)

- Need first and second order moments of decoded pixel value
  - Recursive Formulation (ROPE)

$$E\left\{ \tilde{f}_n^i \right\} = \sum_{\alpha} p(\alpha) \left( E\left\{ \tilde{f}_{n-1}^{i(\alpha)} \right\} + \text{residual}(\alpha) \right)$$

Probability of event  $\alpha$       Expected value of reference pixel

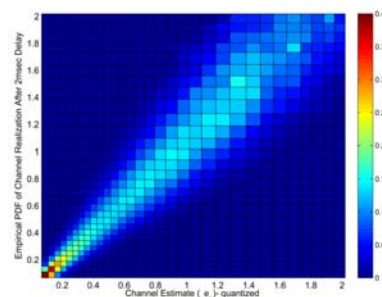
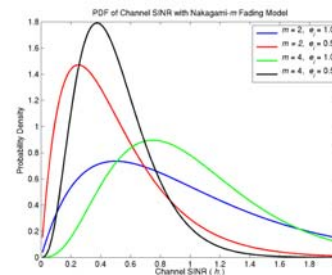
# Outage Probability

- Nakagami- $m$  Fading Model
  - Mean at channel estimate ( $e_i$ )
  - Cumulative cdf at  $h_i$

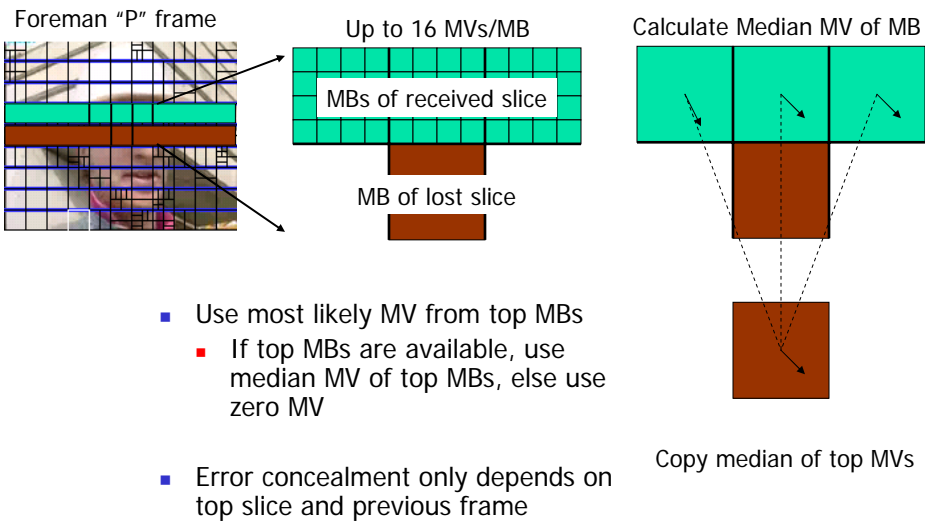
$$\phi_{e_i}(h_i) = \frac{\gamma\left(m, \frac{mh_i}{e_i}\right)}{\Gamma(m)}$$

- Use Empirical Distribution
- Packet Loss Rate

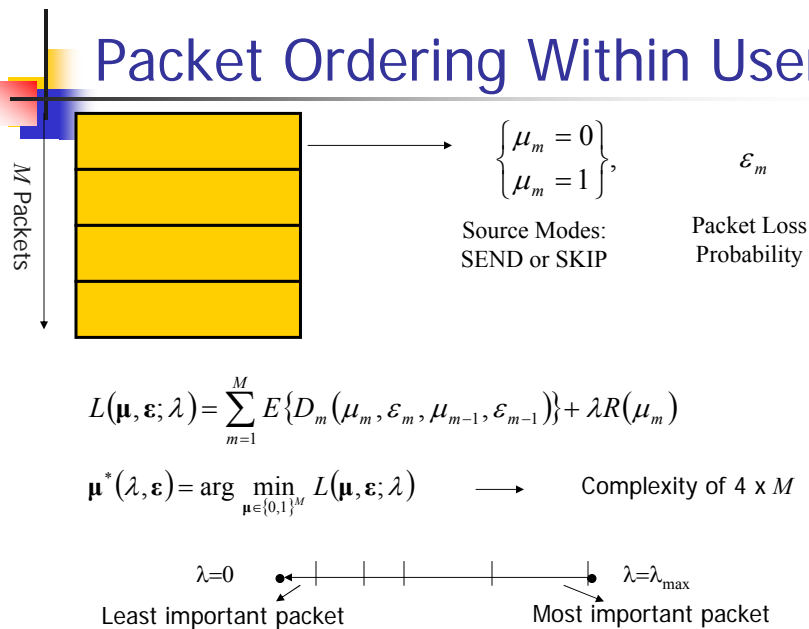
$$\varepsilon_i = \phi_{e_i} \left( \frac{n_i}{p_i} 2^{\frac{r_i}{n_i B} - 1} \right)$$



# Error Concealment Scheme



# Packet Ordering Within User





# Resource Allocation Across Users

At each time slot,

$$\min_{\mathbf{n}, \mathbf{p}, \mathbf{r}} \sum_{i=1}^K ED_i \{r_i, \varepsilon_i(n_i, p_i, r_i, e_i)\}$$

subject to,

$$0 \leq \sum_{i=1}^K p_i \leq P, \quad 0 \leq \sum_{i=1}^K n_i \leq N, \quad 0 \leq n_i \leq N_i, \quad 0 \leq r_i \leq R_{\max_i}$$

$K$  : Number of users;     $\varepsilon_i$  : Probability of loss;     $e_i$  : Channel estimate

$ED_i$  : Expected distortion of user  $i$ 's frame

- Difficult to solve because no simple analytical form exists for  $ED_i$

## Solution – Step I

- First Step – Fix Probability of Loss

- Can write  $r_i$  as function of parameters  $n_i, p_i$

$$r_i = n_i B \log_2 \left( 1 + \frac{p_i \phi_{e_i}^{-1}(\varepsilon_i)}{n_i} \right) \rightarrow \begin{array}{l} \text{Inverse cumulative cdf of} \\ \text{channel SINR conditioned on} \\ \text{estimate } e_i \end{array}$$

- Gradient-Based Solution for Fixed  $\varepsilon_i$

$$\max_{\mathbf{n}, \mathbf{p}} \sum_{i=1}^K -\frac{\partial ED_i}{\partial r_i} \cdot r_i(n_i, p_i)$$

Maximize sum of rates weighted by expected distortion gradients



## Solution – Step II

- Second Step - Fix Resource Allocation ( $n_i^*$ ,

$$p_i^*)$$
$$\varepsilon_i = \phi_{e_i} \left( \frac{n_i^*}{p_i^*} 2^{\frac{r_i^*}{n_i^* B} - 1} \right)$$

- One-Dimensional Search Over Individual User Rates

$$\min_{0 \leq r_i \leq R_{\max_i}} ED_i \{ r_i \} \quad \forall i$$

- Can solve using fast line search method



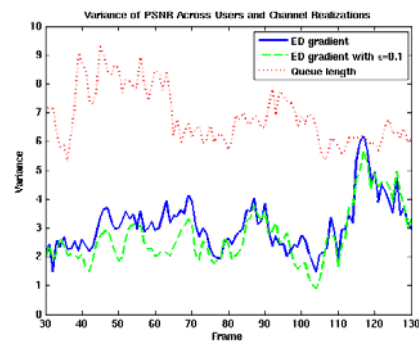
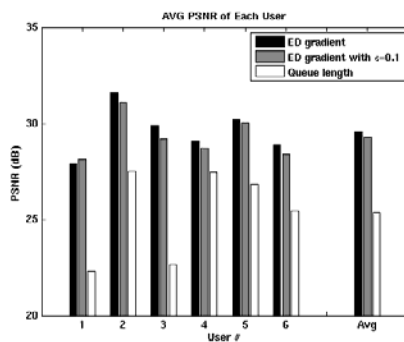
## Implementation Issues

- Acknowledgements
  - Assume ACK/NACK feedback is available for each transmission (MAC layer feedback delay 10msec)
- Packet Fragmentation
  - Application layer packets (i.e., video slices) may be too large to transmit within one timeslot and must be fragmented
  - Assume all fragments of a slice must be received in the correct order, in order to decode the slice
  - Loss probability of a fragmented slice
    - Pr(Any transmitted and not yet ACK/NACK'ed fragment is lost)

## Simulations: Comparison of Metrics

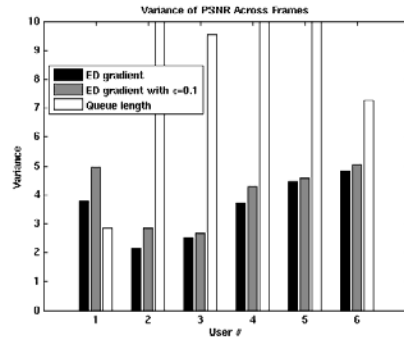
- Distortion Gradient
  - Proposed technique
  
- Distortion Gradient with Fixed Probability of Loss
  - Proposed ordering technique but fix probability of loss
  
- Queue Length
  - Conventional content-independent technique (no packet ordering)
  - Fix probability of loss, and replace gradient of expected distortion with queue length

## Results



- 1: Foreman
  - 2: Mother and daughter
  - 3: Car phone
  - 4: News
  - 5: Hall Monitor
  - 6: Silent
- Packet ordering with expected distortion gradients performs significantly better than queue length method in terms of average and variance of PSNR

# Results



- 1: Foreman
- 2: Mother and daughter
- 3: Car phone
- 4: News
- 5: Hall Monitor
- 6: Silent

- Variance of PSNR across frames within each user is higher when probability of loss is fixed

# Demo

Distortion gradient  
30.7 dB

Distortion gradient  
with fixed loss  
30.0 dB

Queue length  
with fixed loss  
23.7 dB



30.3 dB

29.7 dB

28.6 dB